

Lösningar 110112 Termodynamik för C och D.

1a) $p = p_0 e^{-Mgh/RT} = 1 \text{ atm } e^{-29 \cdot 10^{-3} \cdot 9,81 \cdot 4810 / 8,31 \cdot 273} = 0,55 \text{ atm} = 55 \text{ kPa}$

b) Tefyma: Mättnadstrycket är 55 kPa för 84 °C

2a. $P = Ae\sigma T^4$ ger $T = (P/(Ae\sigma))^{1/4} = (\sin 60^\circ \cdot 900 \text{ W/m}^2 / 1 \cdot 5,67 \cdot 10^{-8} \text{ W/K}^4 \text{m}^2)^{1/4} = 342 \text{ K} = 69 \text{ C}^\circ$

2b. Wiens förskjutningslag ger $\lambda_{max} = 2,898 \cdot 10^{-3} \text{ K} \cdot \text{m} / 342 \text{ K} = 8,5 \text{ } \mu\text{m}$

3a. $Q_{in} = mc\Delta T + mL_f = 20 \text{ kg} (4,19 \cdot 10^3 \text{ J/kgK} \cdot 10 \text{ K} + 333 \cdot 10^3 \text{ J/kg}) = 7,5 \text{ MJ}$

$$W = Q_{in} / K_f = 7,5 / 2,5 \text{ MJ} = 3 \text{ MJ}$$

3b. $Q_{ut} = Q_{in} + W = 7,5 \text{ MJ} + 3 \text{ MJ} = 10,5 \text{ MJ}$

3c. $V_f = Q_{ut} / W = 10,5 / 3 = 3,5$

3d. $7,5 \text{ MJ} \cdot \text{h} / 3600 \text{ s} = 2,1 \text{ kWh}$, skulle kostat 2,1 kr, knappast värt arbetet, investera i värmepump.

4a. $R = \Delta T / P_{före} = 12 \text{ K} / 600 \text{ W} = 0,02 \text{ K/W}$

4b.

$$P_{före} = k_{före} A \Delta T \text{ ger } k_{före} = \frac{P_{före}}{A \Delta T} = \frac{600 \text{ W}}{120 \text{ m}^2 \cdot 12 \text{ K}} = 0,417 \text{ W/m}^2 \cdot \text{K}$$

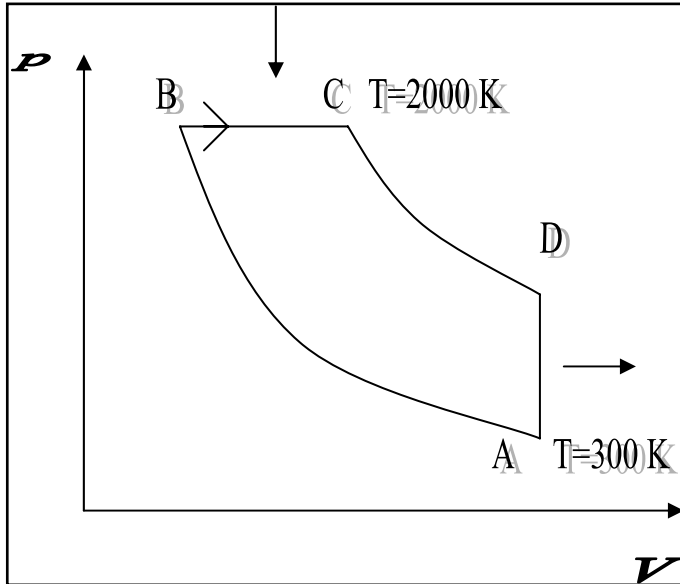
$$\frac{1}{k_{efter}} = \frac{1}{k_{före}} + \frac{L}{\lambda} = \frac{1}{0,417 \text{ W/m}^2 \cdot \text{K}} + \frac{0,1 \text{ m}}{0,04 \text{ W/m} \cdot \text{K}} = 4,90 \text{ m}^2 \text{K/W}$$

$$P_{efter} = k_{efter} A \Delta T = \frac{120 \cdot 12}{4,90} = 294 \text{ W}$$

5a. $m_{is} \cdot L_f = m_v \cdot c_v \cdot \Delta T \Rightarrow m_v = \frac{0,050 \cdot 333 \cdot 10^3}{4190 \cdot 20} \text{ kg} = 199 \text{ g} = 2 \text{ dl}$

b. $\Delta S = \Delta S_{is} + \Delta S_v = \frac{0,050 \cdot 333 \cdot 10^3}{273} \text{ J/K} + 0,199 \cdot 4190 \int_{293}^{273} \frac{dT}{T} = 61,0 \text{ J/K} - 59,0 \text{ J/K} = 2,0 \text{ J/K}$

6.



$$\eta = 1 - \frac{Q_{out}}{Q_{in}} = 1 - \frac{2,5 \cdot nR(T_D - T_A)}{3,5 \cdot nR(T_C - T_B)}, \quad r = \frac{V_A}{V_B} = 18, \quad V_A = V_D, \quad p_B = p_C$$

$$A \rightarrow B \text{ adiabat, Poisson: } T_B = T_A \left(\frac{V_A}{V_B} \right)^{\gamma-1} = T_A \cdot r^{\gamma-1} = 300 \text{ K} \cdot 18^{0,4} = 953,3 \text{ K}$$

$$B \rightarrow C \text{ isobar: } V_C = V_B \left(\frac{T_C}{T_B} \right) = \left(\frac{V_A}{r} \right) \cdot \left(\frac{T_C}{T_A r^{\gamma-1}} \right)$$

$$C \rightarrow D \text{ adiabat Poisson: } T_D = T_C \left(\frac{V_C}{V_D} \right)^{\gamma-1} = T_C \left(\frac{T_C}{T_A r^{\gamma}} \right)^{\gamma-1} = 2000 \text{ K} \left(\frac{2000}{300 \cdot 18^{1,4}} \right)^{0,4} = 846,5 \text{ K}$$

$$\eta = 1 - \frac{2,5(846,5 - 300)}{3,5(2000 - 953,3)} = 0,63$$